

# LECTURE 1: GENERAL RELATIVITY

• SPACETIME AND GEOMETRY: AN INTRODUCTION TO GENERAL RELATIVITY  
 BY SEAN M. CARROL

• OVERVIEW

- Special Relativity and Minkowski Space
- TENSOR CALCULATION, the musical notations
- Energy, Momentum, 4-vectors and Physics
- Lagrangian formalism & Classical field theory
- Manifolds: calculus on curved space (Chapter 2)

$$M = \mathbb{R}^4 \text{ paired with Minkowski metric}$$

$$\langle v, w \rangle = v^\mu w^\nu \eta_{\mu\nu}$$

$$g = g_{\mu\nu} dx^\mu \otimes dx^\nu$$

- CURVATURE (Chapter 3)

covariant derivative  
 parallel transport  
 geodesics  
 Riemann curvature tensor

$$\frac{d^2 X^\mu}{d\lambda^2} + \Gamma^\mu_{\rho\sigma} \frac{dX^\rho}{d\lambda} \frac{dX^\sigma}{d\lambda} = 0$$

- GRAVITATION: - Einstein's field eqs and their properties (Chapter 4)

- Equivalence principle  
 - alternate theories

$$R_{\mu\nu} - \frac{1}{2} R g_{\mu\nu} = 8\pi G T_{\mu\nu}$$

- Schwarzschild Solution: properties, singularity, black holes (Chapter 5)

- GRAVITATIONAL RADIATION: - linearized gravity (Chapter 7)

- gauge conditions  
 - gravitational waves

- COSMOLOGY: - maximally symmetric universes (Chapter 8)

- Robertson-Walker metrics  
 - dark matter, cosmological constant...  
 - inflation

• Additional Resources:

- MTW
- Weinberg
- Lawson
- Wald
- Dynamics & Relativity by McComb
- Schutz
- Resnik }
- Rindler } SR