MATH 200 MISSION 1: LOGIC

Working together is encouraged, share ideas not calculations. Explain your steps. This sheet must be printed and attached to your assignment as a cover sheet. The calculations and answers should be written neatly on one-side of paper which is attached and neatly stapled in the upper left corner. No fuzzies thanks. Box your answers where appropriate. Please do not fold. Thanks!

- Problem 1 Restate each statement below as an implication using the words "If... then ..."
 - (a.) Whenever a function is a polynomial, it's continuous.
 - (b.) An exponential function must be positive.
 - (c.) A prime number greater than two cannot be even.
 - (d.) A differentiable function necessarily has a derivative.
- **Problem 2** Consider the sentence: If a cat is good then 0 = 1. Given that all cats are not good, decide if the given sentence is true.
- **Problem 3** Suppose P, Q are true while S and T are false. Determine if the following compound statements are true or false,
 - (a.) $(P \vee S) \wedge (Q \vee T)$
 - **(b.)** $(P \wedge S) \vee (Q \wedge T)$
 - (c.) $(P \wedge Q) \Rightarrow (S \wedge T)$
 - (d.) $P \land \sim Q \Rightarrow \sim S$
- **Problem 4** Consider the following statement: "Goku has a flying nimbus, but his wife does not." Give appropriate definitions for a and b and translate our statement into a formal proposition in terms of a and b. Define and translate in such a way that your logical statement involves at least one negation.
- **Problem 5** Let a be the statement "Tomorrow is judgement day", b be "The cat is a robot", and c be "Trogdor burns the countryside". Write down a plain English version of the proposition using these translations of a, b, and c.
 - (a.) Proposition #1: $a \lor \sim b$
 - **(b.)** Proposition #2: $(a \land \sim b) \Rightarrow c$
 - (c.) Proposition #3: $\sim a \land (b \Rightarrow c)$
- **Problem 6** Prove $P \lor (Q \land R) \equiv (P \lor Q) \land (P \lor R)$
- **Problem 7** Prove $\{ \sim (P \vee Q) \} \equiv \{ \sim P \land \sim Q \}$
- **Problem 8** Prove $[P \land (P \Rightarrow Q)] \Rightarrow Q$ is a tautology.
- **Problem 9** Prove $[P \Rightarrow (Q \land \sim Q)] \Leftrightarrow \sim P$ is a tautology.
- **Problem 10** Prove $\{(P \land Q) \Rightarrow R\} \equiv \{ \sim R \Rightarrow (\sim P \lor \sim Q) \}$
 - (a.) via a truth table proof,
 - (b.) via a column commented symbolic logic proof.