Math 231 Mission 6

Copying answers and steps is strictly forbidden. Evidence of copying results in zero for copied and copier. Working together is encouraged, share ideas not calculations. Explain your steps. This sheet must be printed and attached to your assignment as a cover sheet. The calculations and answers should be written neatly on one-side of paper which is attached and neatly stapled in the upper left corner. Box your answers where appropriate. Please do not fold. Thanks!

Problem 101 Your signature below indicates you have:

- (a.) I have read Chapter 6 of Cook:
- (b.) I have attempted homeworks from Salas and Hille as listed below:

The following homeworks from the text are good rudimentary skill problems. These are not collected or graded. However, they are all usually odd problems thus there are answers given within Salas, Hille and Etgen's text:

$$\S 16.7 \#$$
's 1, 5, 9, 13, 21, 29, 35, 36, 42, 53

$$\S 16.10 \#$$
's 3, 11, 17, 25, 30

Problem 102 Let a, b be constants. Calculate $\int_0^a \int_0^b (2x + 4y) dx dy$.

Problem 103 Calculate
$$\int_0^{\pi/2} \int_0^{\pi/2} \left(\sin(x) + \cos(y)\right) dx \, dy.$$

Problem 104 Let a, b be constants. Calculate $\int_0^{\ln(a)} \int_0^{\ln(b)} e^{x+y} dx dy$.

Problem 105 Calculate
$$\int_{-1}^{1} \int_{0}^{1} \sin^{p}(x) \cos^{42}(y) dy dx$$
 where $p > 2$ is a prime.

Problem 106 Calculate the average of $f(x,y) = x^2 + y^2$ on the unit-square $Q = [0,1] \times [0,1]$.

Problem 107 Calculate the average of $f(x,y) = x^2 + y^2$ on the triangle T with vertices (0,0), (1,2) and (2,0).

- **Problem 108** Suppose $\iint_R f dA = \int_0^1 \int_{x^2}^x (1+x) dy dx$. Calculate the given integral.
- **Problem 109** For the integral given in the previous problem, explicitly write R as a subset of \mathbb{R}^2 using set-builder notation. In addition, calculate the integral once more with the interation of the integrals beginning with dx. Draw a picture to explain the inequalities which form the basis for your new set-up to the integral.
- **Problem 110** Reverse the order of integration in order to calculate the following integral:

$$\int_0^1 \int_y^1 \frac{2}{1+x^4} \, dx \, dy.$$

- **Problem 111** Let B be the solid region bounded by x = 0, y = 0, z = 0 and the plane 2x + 2y 3z = 1. Calculate the volume of B.
- **Problem 112** Let R be the region bounded by $x^2 + y^2 = 1$ and $x^2 + y^2 = 4$ and y = x and y = 3x. Calculate $\iint_R \sqrt{x^2 + y^2} \, dA$ by changing the integration to polar coordinates.
- **Problem 113** Find the center of mass of the region Ω inside the circle $r = 2 \sin \theta$ and outside the circle r = 1 given mass-density $\sigma(x, y) = y$. (Salas and Hille used λ for density in §16.5)
- **Problem 114** Let B be the region bounded by $\phi = \pi/2$ and $\phi = \pi/4$. Calculate $\iiint_B x^2 dV$.
- **Problem 115** Find the volume bounded by the cylinder $x^2 + y^2 = 1$ and z = 2 + x + y and z = 1.
- **Problem 116** Let B be a ball of radius R centered at the origin. Calculate $\iiint_B e^{-\rho^3} dV$.
- **Problem 117** Let $u = x^2 + y^2$ and $v = x^2 z^2$ and w = xyz calculate $\frac{\partial(x,y,z)}{\partial(u,v,w)}$.
- **Problem 118** Find the volume of a ball of radius R with the top cap of height h is removed. You should assume h is measured along a diameter of the ball and h < R.
- **Problem 119** Calculate $\iint_R \sqrt{x+y} \sin(2x-y) dA$ where $R = [0,1] \times [0,1]$ by making an appropriate change of variables.
- Problem 120 Show your work for Problem #36 of §16.7 in Salas and Hille's Eighth Edition.